



มหาวิทยาลัยราชภัฏนครปฐม
Nakhon Pathom Rajabhat University

Chapter 3

Projectile Motion

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Stand 4 : Force and Motion

Standard Sc. 4.2 Understand the characteristics of motion of objects natural quest for knowledge and psychology, science communicating what is learn and put the knowledge to use.





Class	Indicators	Learning core
M. 4-6	2. Observe and describe the Projectile motion, Circular and Simple Harmonic.	<ul style="list-style-type: none">- Projectile motion as a movement trajectory curve with speed on the horizontal stabilizers and the acceleration in the vertical stabilizers.- Circular motion is moving with speed lines touch the circle and there is a force in the direction towards the center.- Simple Harmonic motion as moving go and back repeatedly Ex. The swing of the simple pendulum by the angle of maximum deviation from vertical has a constant throughout
	3. Discussion the results of the query and benefit about Projectile Motion, Circular and Simple Harmonic.	<ul style="list-style-type: none">- The Projectile Motion can be utilized Ex. Playing tennis, Basketball.- The circular movement can be utilized Ex. The curved way of drive car to be safety.- The Simple Harmonic motion can be utilized for building a clock pendulum.



Motion

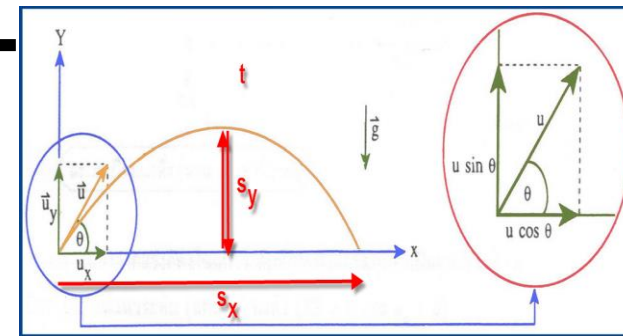
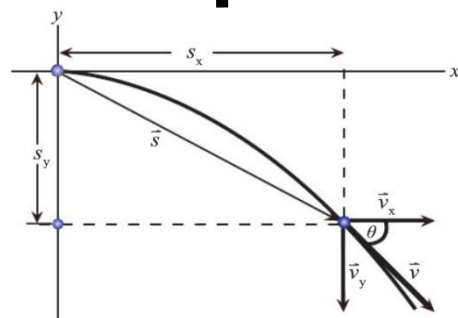
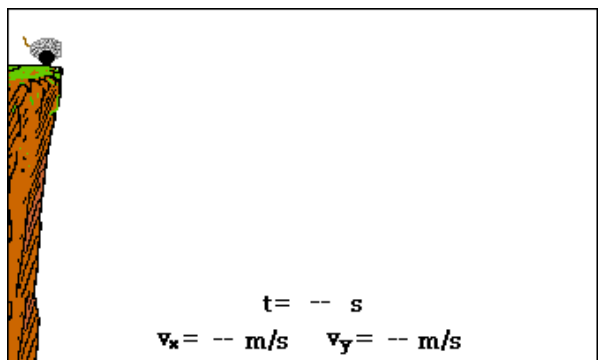
Projectile
motion

Circular
motion

Simple
harmonic
motion



Projectile Motion



Horizontal motion

$$s_x = v_x t$$

$$s_y = \left(\frac{u_y + v_y}{2} \right) t$$

Vertical motion

$$s_y = u_y + gt$$

$$s_y = u_y t + \frac{1}{2} g t^2$$

$$v_y^2 = u_y^2 + 2gs_y$$

Displacement

$$s = \sqrt{s_x^2 + s_y^2}$$

$$\tan \alpha = \frac{s_y}{s_x}$$

Velocity

$$v = \sqrt{v_x^2 + v_y^2}$$

$$\tan \theta = \frac{v_y}{v_x}$$

Horizontal

$$s_x = u_x t$$

$$s_x = (u \cos \theta) t$$

Vertical

$$s_y = u_y t + \frac{1}{2} a_y t^2$$

$$s_y = (u \sin \theta) t - \frac{1}{2} g t^2$$



Distance
(s)

Length along the path
that all moving objects.

Displacement
(\vec{s})

The object moves from
the starting position to
the final position.

**Initial
velocity (u)**

Speed at the beginning.

**Final
velocity (v)**

Speed at the ending.



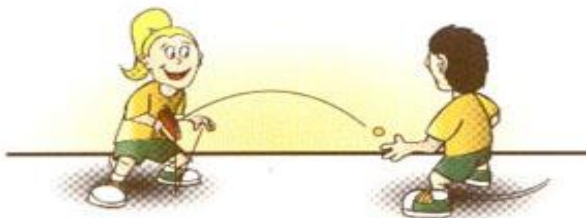
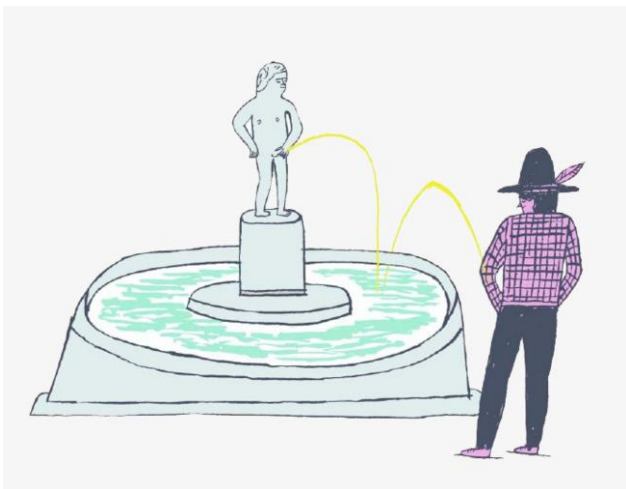
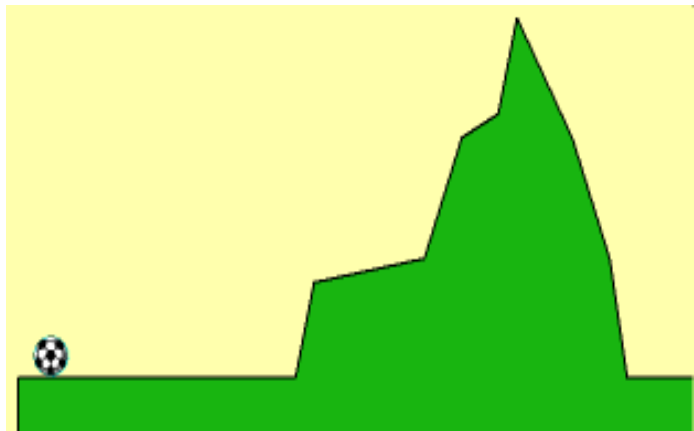
Gravitation force (g)

The acceleration to the gravity of the world and a direction perpendicular to the ground, the world.





N P R U

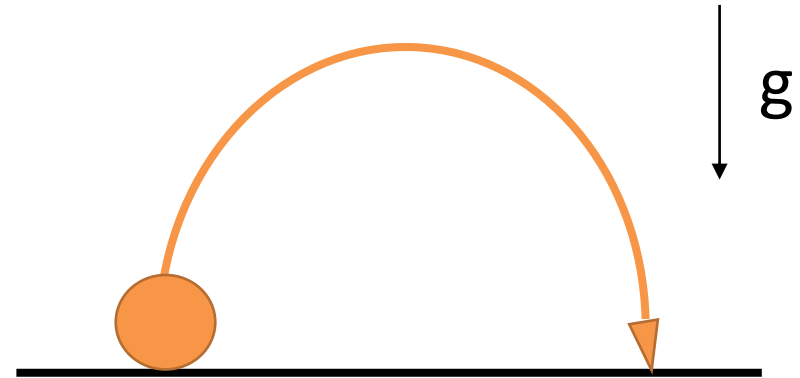
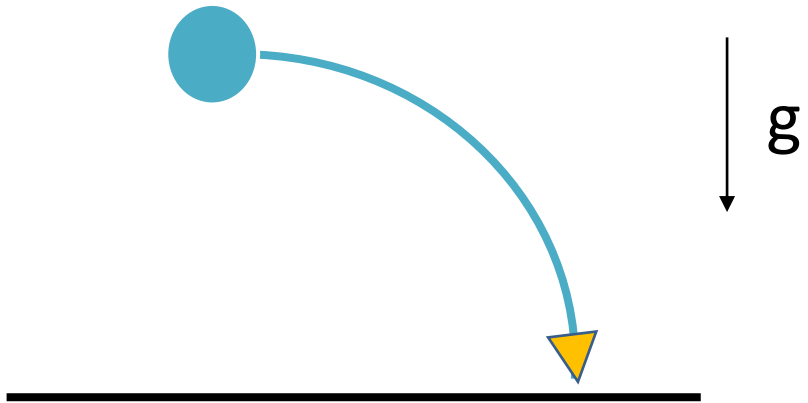




The Projectile motion

If consider the Projectile motion of the steel ball was throw by weight watchers or the movement of basketball was throw, will find that the movement is curved.





$$a=g$$

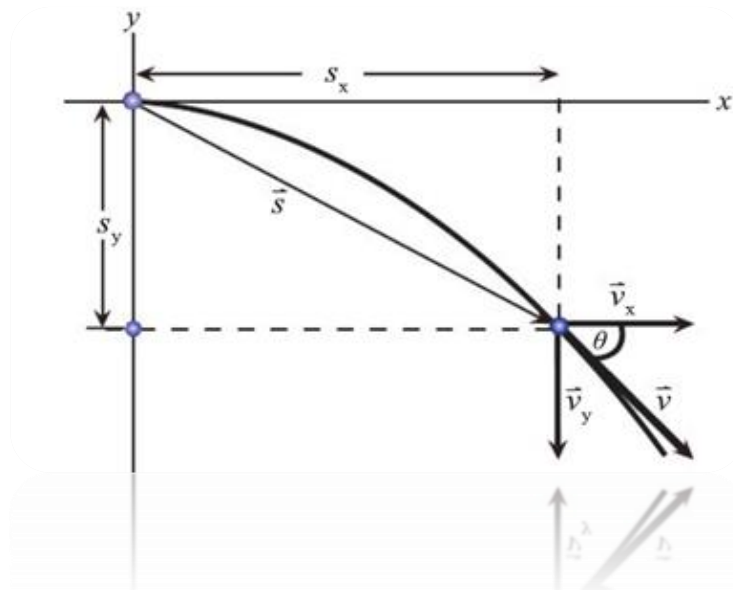


Horizontal motion and Vertical motion



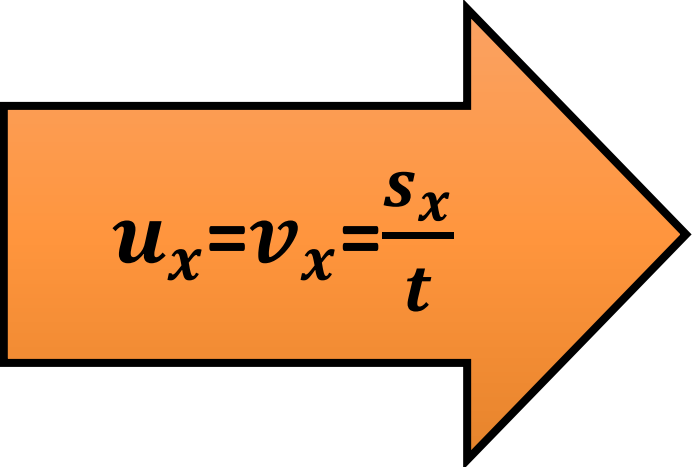
Horizontal motion

Horizontal movement the object was hurl out on unchanged the horizontal movement because resultant force in the horizontal movement acts on the object is zero, by assume air resistance is worth very little until not be calculated.





Horizontal Direction Calculations


$$u_x = v_x = \frac{s_x}{t}$$

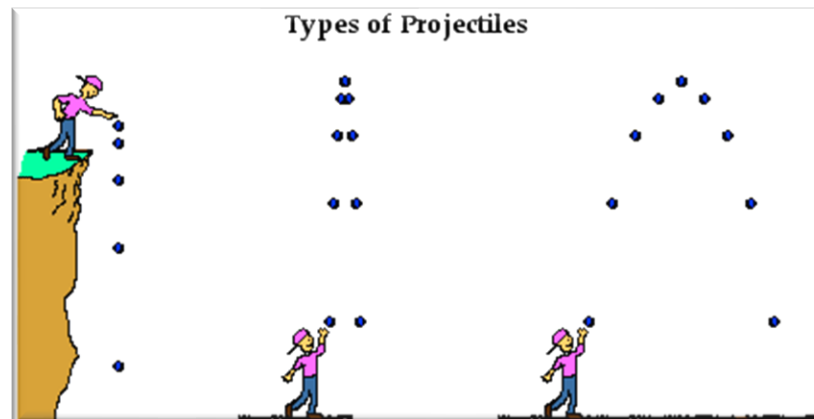
$$s_x = v_x t$$

s_x : Horizontal displacement.
 u_x : Horizontal initial velocity.
 v_x : Horizontal final velocity.
 t : Time.



Vertical motion

Horizontal movement the object was hurl out on unchanged the horizontal movement because resultant force in the horizontal movement acts on the object is zero, by assume air resistance is worth very little until not be calculated.





Vertical Direction Calculations

$$s_y = u_y + gt$$

$$s_y = u_y t + \frac{1}{2}gt^2$$

$$v_y^2 = u_y^2 + 2gs_y$$

$$s_y = \left(\frac{u_y + v_y}{2} \right) t$$

s_y : Vertical displacement.

u_y : Vertical initial velocity.

v_y : Vertical final velocity.

g : The value of acceleration where with gravity.

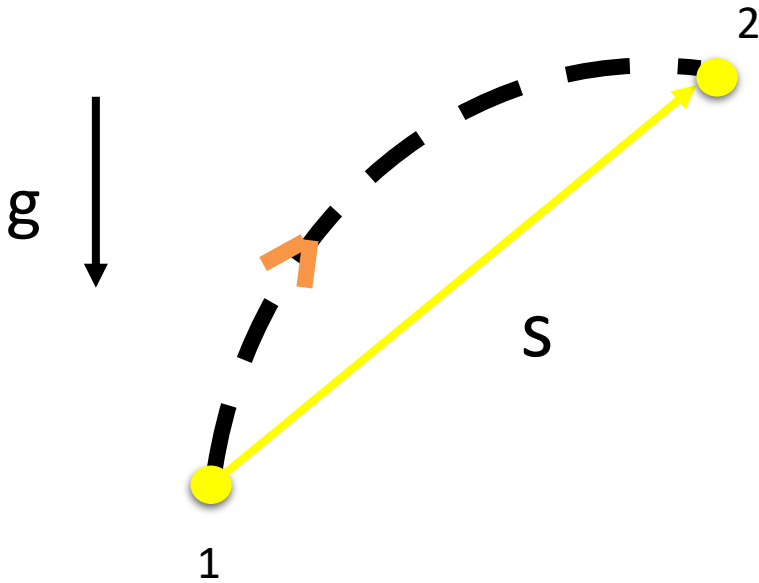
t : Time



Displacement and Velocity of The Object



Displacement and Acceleration of The Object



$$S = \sqrt{s_x^2 + s_y^2}$$

$$\tan \alpha = \frac{s_y}{s_x}$$

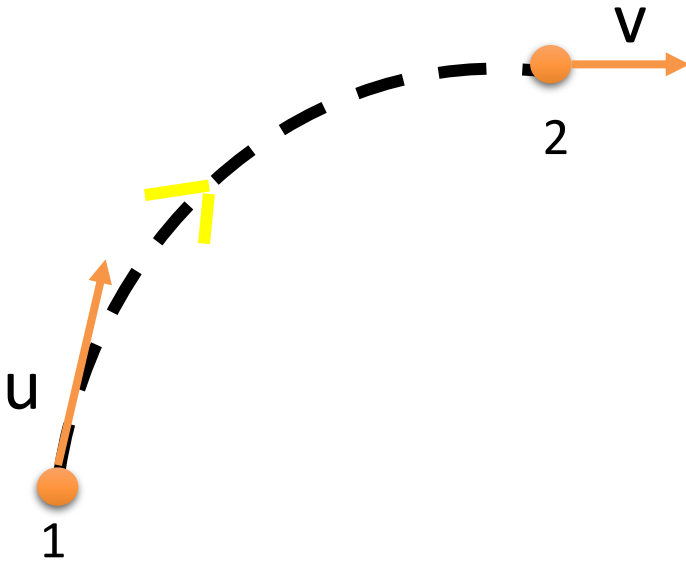
S_x : Horizontal displacement of the object measured from the beginning.

S_y : Vertical displacement of the object measured from the beginning.

S : Displacement resultant force of the object measured from the beginning.



Velocity of the object



$$v = \sqrt{v_x^2 + v_y^2}$$

$$\tan \theta = \frac{v_y}{v_x}$$

v_x : Velocity of the object horizontal.

v_y : Velocity of the object vertical.

v : Velocity resultant force of the object in tangent.

θ : Corner resultant force of the object in tangent do with horizontal.



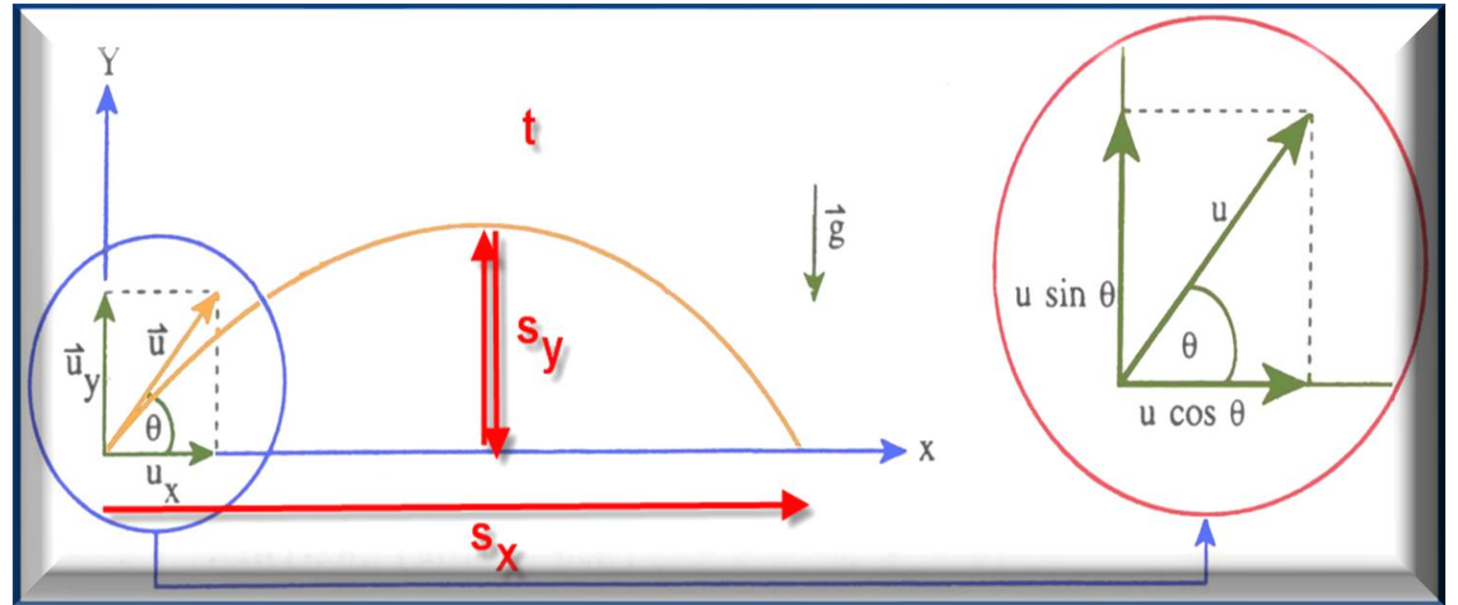
**Object of Velocity initial velocity corner
with horizontal lines**



Horizontal

$$s_x = u_x t$$

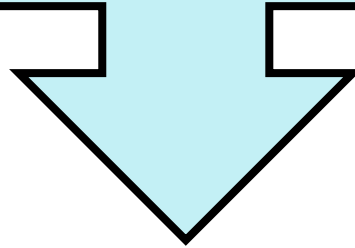
$$s_x = (u \cos \theta) t$$





The Horizontal movement

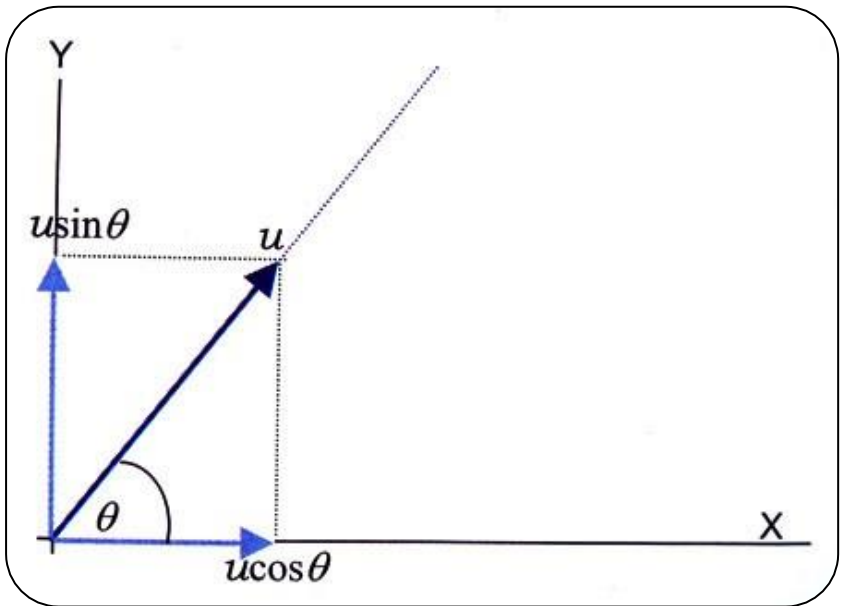
- u_x : The speed in the horizontal streak.
- s_x : The displacement in the horizontal streak.
- t : Time of the movement.



Size displacement in a horizontal streak s_x or the distance an object moving in a horizontal streak from the start until the fall to the same ground level call it **Rang** of object.



Vertical



$$s_y = u_y t + \frac{1}{2} a_y t^2$$

$$s_y = (u \sin \theta) t - \frac{1}{2} g t^2$$



The vertical movement

u_y : The vertical $u_y = \mathcal{U} \sin \theta$

a_y : The vertical acceleration equal to $-g$

s_y : The vertical displacement.

t : Time of the vertical movement equal to time of the horizontal movement.

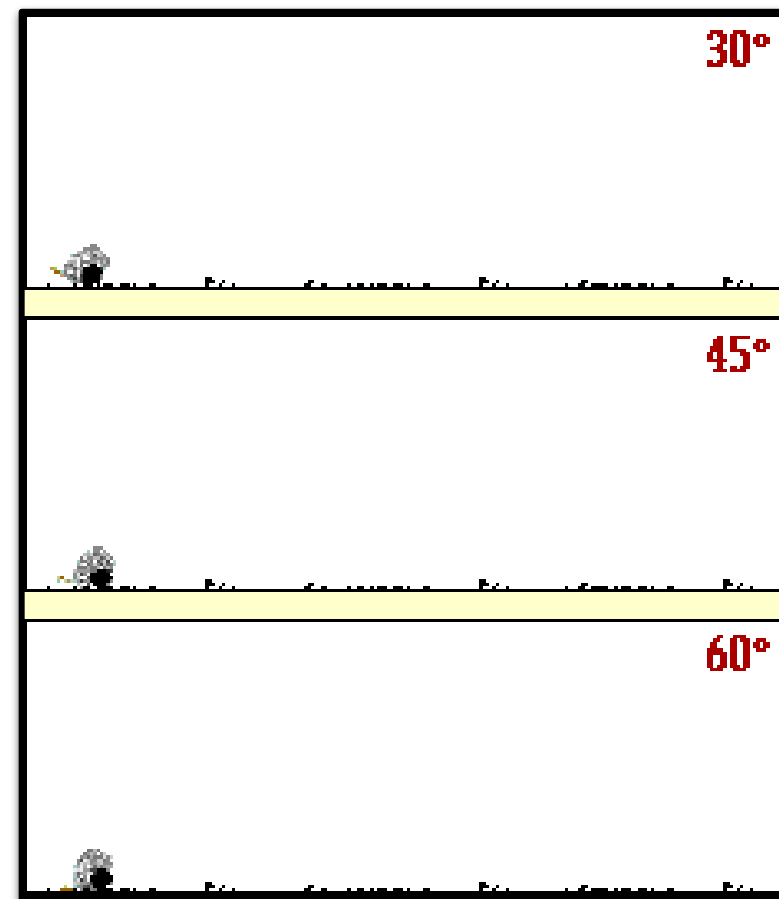


NOTE:

$$s_y = 0$$
$$0 = (u \sin \theta - \frac{1}{2} g t) t$$

$t = 0 :$

$$t = \frac{2u \sin \theta}{g}$$





The End