



# Physics of Engineer

## Chapter 9: Mechanics of Particle and Rigid Body

Kittipong Siengsanoh (Ph.D.Physics)

Department of Physics

Faculty of Science and Technology

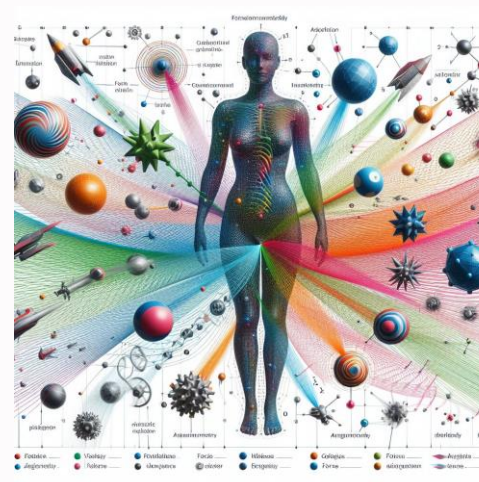


# Outline

- Introduction to Mechanics of Particles and Rigid Bodies
- Particles
- Kinematics of a Particle
- Equation of Motion
- Sample Application
- Rigid Bodies
- Force and Newton's Laws
- Kinetics of Rigid Body
- Translational Motion of a Rigid Body

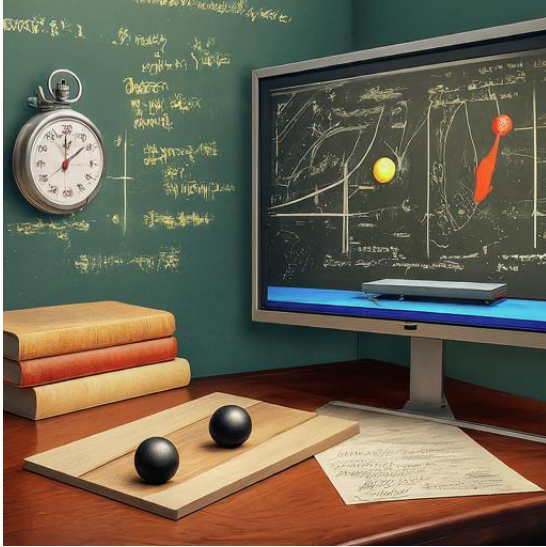
# Outline

- Rotational Motion of a Rigid Body
- Application of Rotational Motion
- Conclusion
- Exploring Resources and references





# Introduction to Mechanics of Particles and Rigid Bodies



## What is Mechanics?

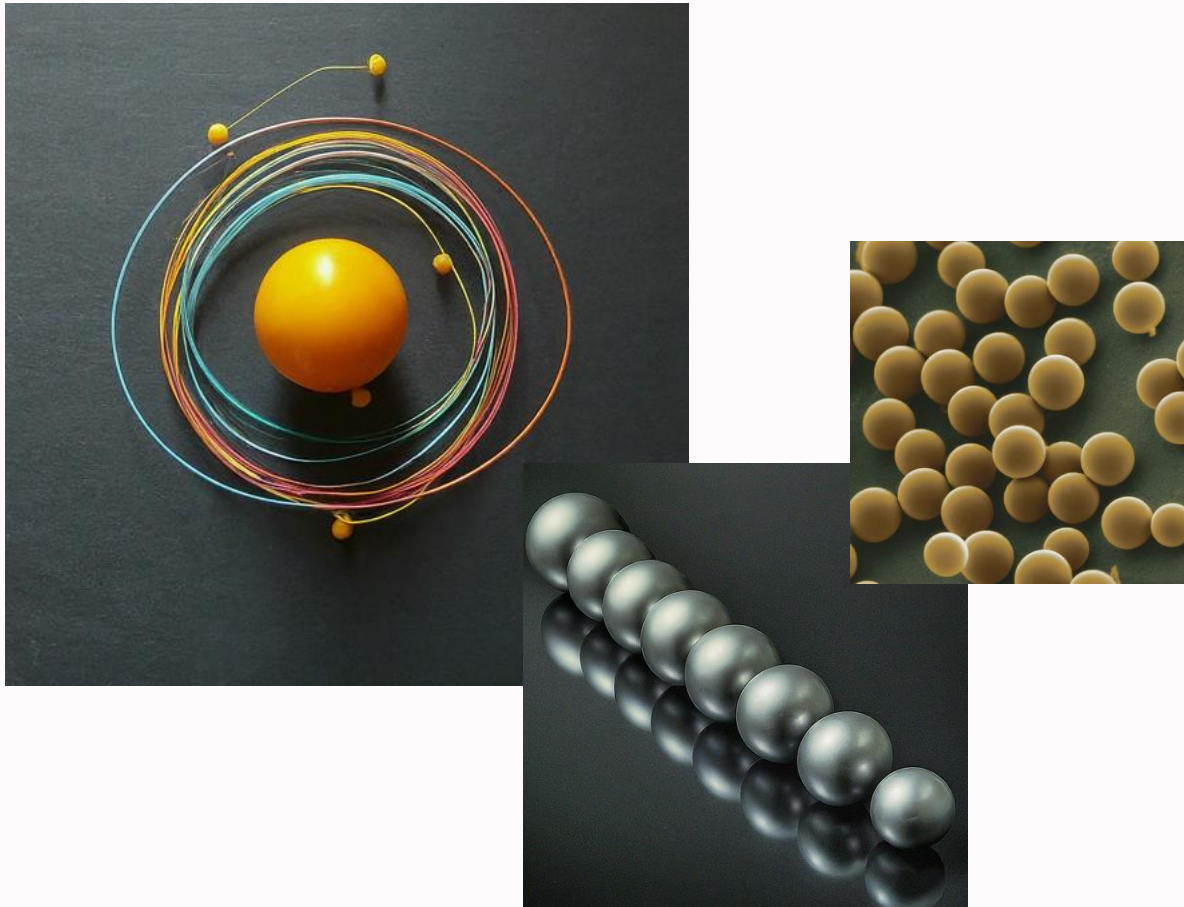
- The study of motion and its causes.

## Sub-disciplines of Mechanics:

- Kinematics: Description of motion.
- Kinetics: Analysis of forces causing motion.



# Particles



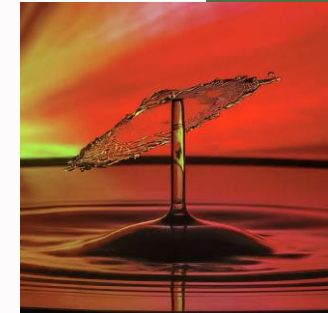
- **Definition:** A point-like object with a mass but negligible size.
- **Parameters:**
  - Mass ( $m$ ): Quantity of matter, measured in kilograms (kg).

04



# Kinematics of a Particle

- Description of motion of a particle.
- Parameters:
  - **Position vector ( $\mathbf{r}$ ):** Location of the particle relative to a reference point, denoted by an arrow ( $\rightarrow$ ). Measured in meters (m).
  - **Displacement ( $\Delta\mathbf{r}$ ):** Change in position vector over a time interval.  $\Delta\mathbf{r} = \mathbf{r}_f - \mathbf{r}_i$  (final position minus initial position).
  - **Velocity ( $\mathbf{v}$ ):** Rate of change of position vector.  $\mathbf{v} = \Delta\mathbf{r} / \Delta t$  (displacement divided by time interval). Measured in meters per second (m/s).
  - **Acceleration ( $\mathbf{a}$ ):** Rate of change of velocity.  $\mathbf{a} = \Delta\mathbf{v} / \Delta t$  (change in velocity divided by time interval). Measured in meters per second squared (m/s<sup>2</sup>).



# Equations of Motion

- Relate the kinematic parameters of a particle.
- 1D Motion with constant acceleration:

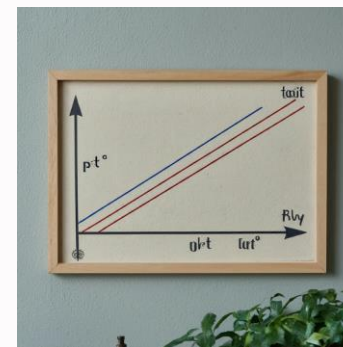
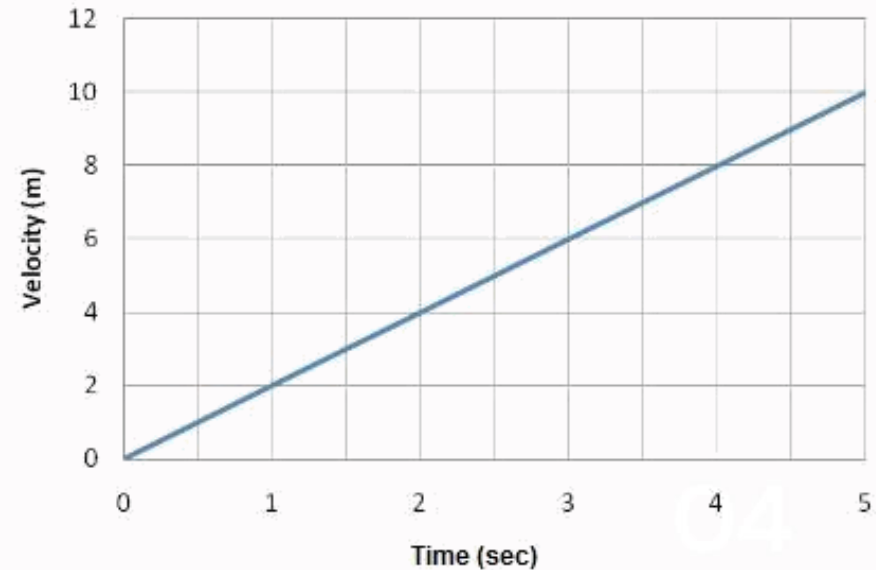
$$v = u + at$$

(final velocity = initial velocity + acceleration × time)

$$s = ut + \frac{1}{2} at^2$$

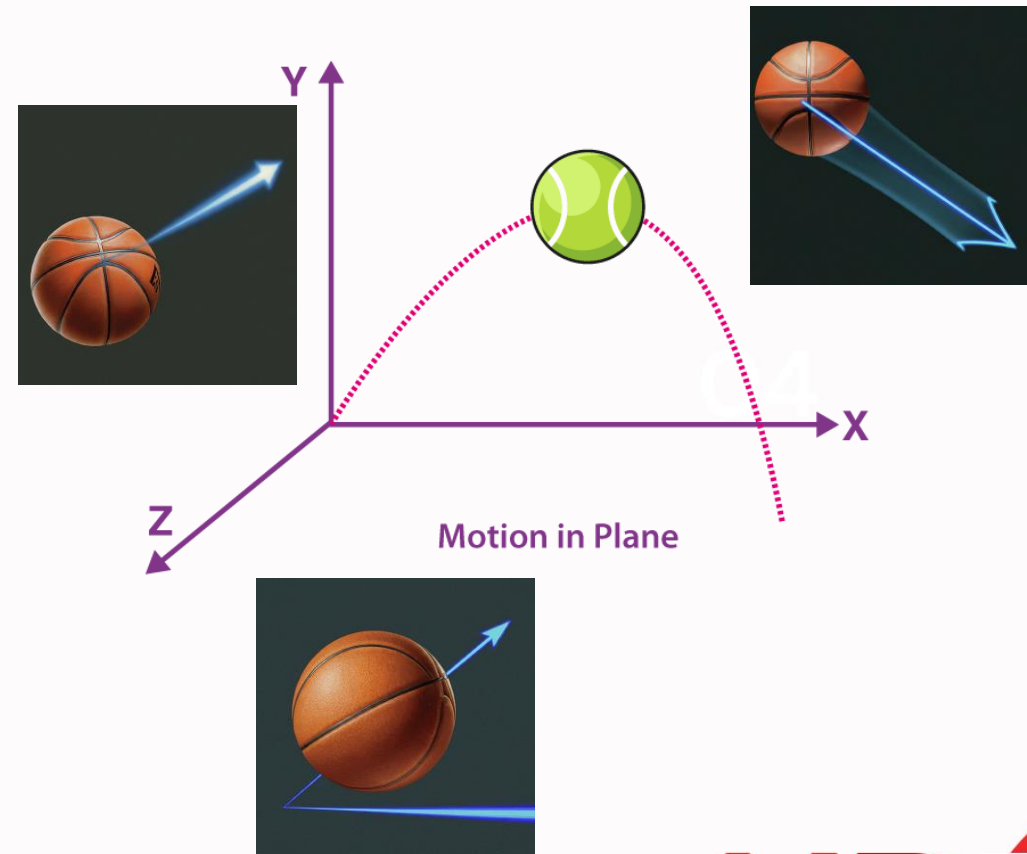
(displacement = initial velocity × time +  $\frac{1}{2}$  × acceleration × time<sup>2</sup>)

### Constant Acceleration



# Sample Application: Projectile Motion

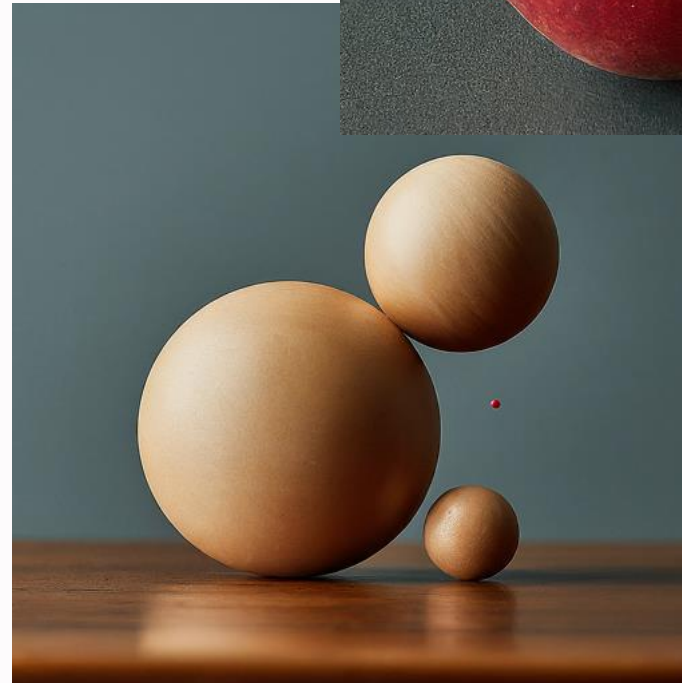
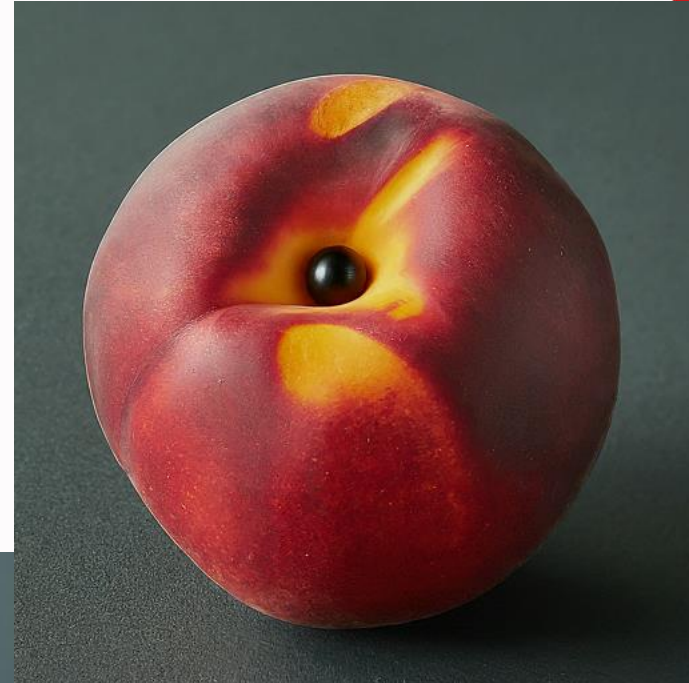
- A thrown object neglecting air resistance.
- Motion is a combination of horizontal and vertical components.
- Horizontal motion: Constant velocity (no horizontal force).
- Vertical motion: Constant acceleration due to gravity ( $g \approx 9.8 \text{ m/s}^2$ ).





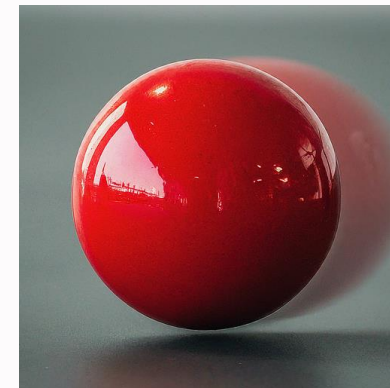
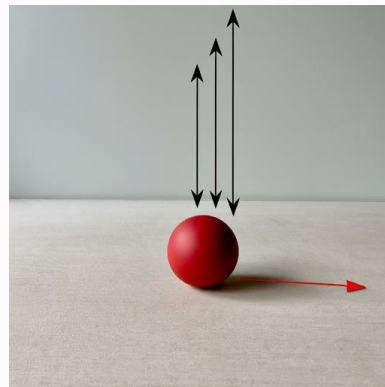
# Rigid Bodies

- **Definition:** An object with a fixed, non-deformable shape and a distribution of mass.
- **Parameters:**
  - Mass ( $m$ ): Total mass of the rigid body (same as for a particle).
  - Center of Mass (COM): The point where the entire mass of the body can be considered concentrated. Denoted by  $CM$ .



# Forces and Newton's Laws

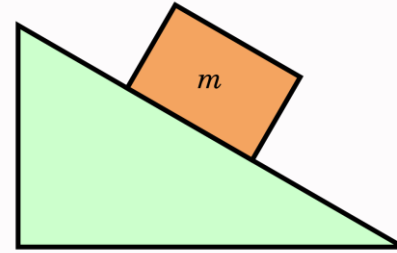
- **Force:** An interaction that can cause an object to change its state of motion (measured in Newtons, N).
- **Newton's Laws of Motion:**
  - First Law (Law of Inertia): An object at rest stays at rest and an object in motion stays in motion with constant velocity unless acted upon by a net force.
  - Second Law (Law of Acceleration): The acceleration of an object is directly proportional to the net force acting on it and inversely proportional to its mass ( $a = F_{\text{net}} / m$ ).



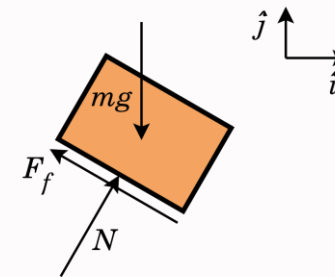
# Newton's Laws (Continued)

- Third Law (Law of Action-Reaction): For every action, there is an equal and opposite reaction force.
- Free Body Diagram (FBD):
  - A diagram showing all forces acting on a body.

A block on a ramp



Free body diagram of just the block



04

# Kinetics of a Rigid Body

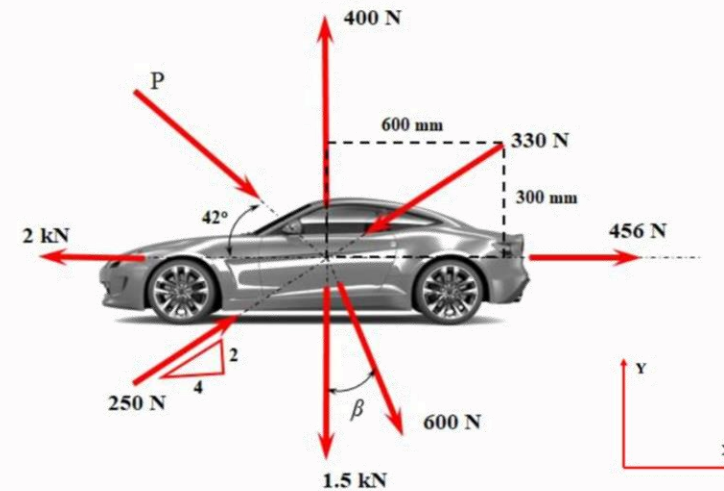
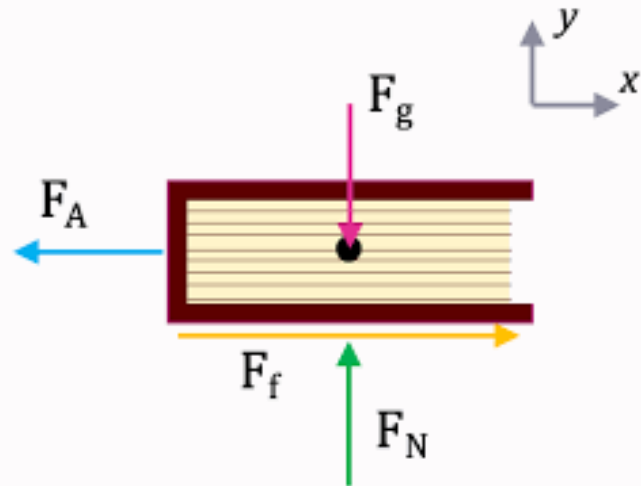
- Rigid body motion can be described by the motion of its center of mass (COM).
- Two types of motion for a rigid body:
  - Translation: Movement of the COM without any rotation.
  - Rotation: Movement about a fixed axis or point.



04



# Translational Motion of a Rigid Body



04

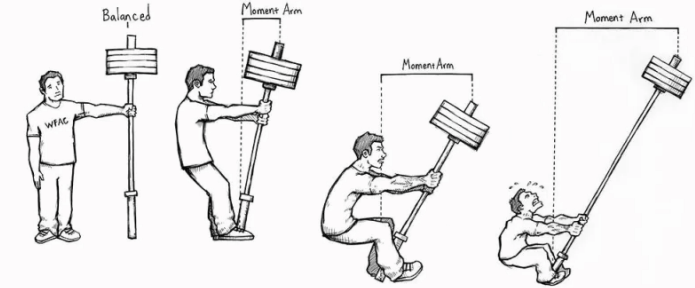
- Analyzed using the same concepts as for a particle (Newton's Laws, FBDs).
- COM acts as a point-like mass for translational motion.

# Rotational Motion of a Rigid Body

- **Torque ( $\tau$ ):** Rotational equivalent of force.

$$\tau = r \times F$$

(torque = moment arm  $\times$  force), where  $r$  is the distance from the axis of rotation to the line of action of the force.



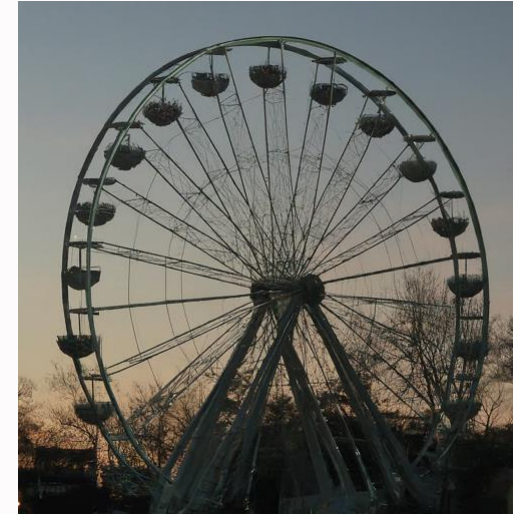
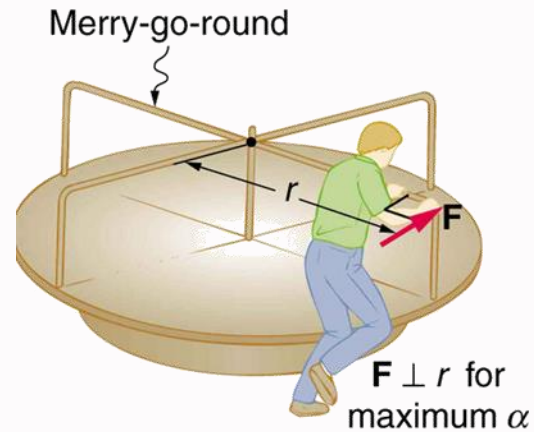
- **Angular momentum ( $L$ ):** Measure of an object's rotational inertia.

$$L = I\omega$$

(angular momentum = moment of inertia  $\times$  angular velocity), where  $I$  is the moment of inertia and  $\omega$  is the angular velocity.

- **Moment of inertia ( $I$ ):** Distribution of mass within a rigid body that resists changes in its rotational state.

# Applications of Rotational Motion



- Everyday examples of rotational motion and torque (e.g., opening a door, Ferris wheel).
- Problem-solving using torque and angular momentum.



# Conclusion

## Content:

Summarize the main concepts covered in the presentation:

- Kinematics of particles (motion description)
- Kinetics of particles and rigid bodies (forces and motion)
- Applications of mechanics in various scenarios (equilibrium, friction, work & energy, conservation laws)

Importance of understanding mechanics:

- Foundational concept in physics
- Explains motion of objects in our world
- Applicable in various engineering and technological fields

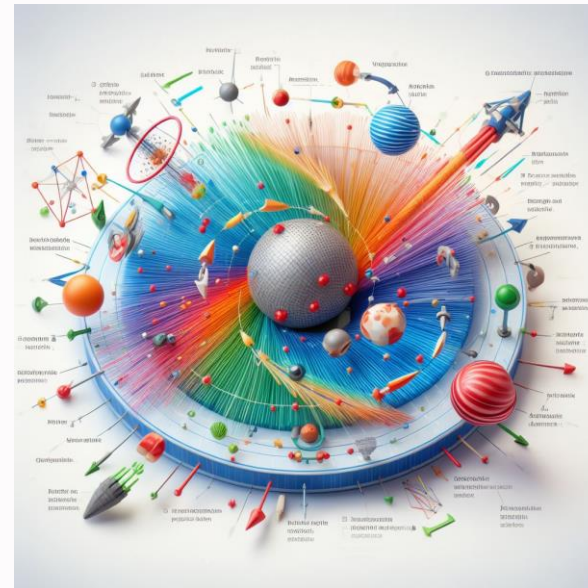
04



# Conclusion

## Concluding Statement:

- Mechanics provides a powerful framework for analyzing motion and its causes. By understanding these principles, you can gain a deeper appreciation for the physical world around you.





# Exploring Resources and References

## Textbooks:

### Introductory Level:

- Mechanics by Randall D. Knight (Pearson) ([Link to bookstore or publisher website]) - This widely used textbook provides a clear and concise introduction to mechanics, covering both particles and rigid bodies.
- An Introduction to Mechanics by Daniel Kleppner and Robert Kolenkow (Dover Publications) ([Link to bookstore or publisher website]) - A classic text offering a thorough and rigorous approach to mechanics, suitable for students seeking a deeper understanding.

### Intermediate Level:

- Classical Mechanics by Herbert Goldstein, Charles P. Poole, and John L. Safko (Pearson) ([Link to bookstore or publisher website]) - A comprehensive and advanced text, covering classical mechanics concepts in detail. (Consider recommending this for students interested in a deeper dive after mastering the basics.)
- Analytical Mechanics by Louis N. Hand and Janet D. Finch (Cambridge University Press) ([Link to bookstore or publisher website]) - Another advanced text with a strong focus on the mathematical analysis of mechanics. (Similar to the previous one, this might be suitable for highly motivated students.)



# Exploring Resources and References

## Exploring Online Resources:

- Websites: Include links to reputable websites: (e.g., Khan Academy: <https://www.khanacademy.org/science/physics>, MIT OpenCourseware: <https://ocw.mit.edu/>)
- Simulations: Suggest interactive simulations related to mechanics concepts. (e.g., PhET Interactive Simulations: <https://phet.colorado.edu/en/simulations/browse>)

## Reference:

- Tipler, P. A., & Mosca, G. (2003). Physics for Scientists and Engineers: Mechanics, Oscillations and Waves, Thermodynamics (Vol. 1). W. H. Freeman.
- Khan Academy. (n.d.). Mechanics. Retrieved from <https://www.khanacademy.org/science/physics>

04



# Physics of Engineer

## Chapter 9: Mechanics of Particle and Rigid Body

Kittipong Siengsanoh (Ph.D.Physics)

Department of Physics

Faculty of Science and Technology